

# **Before Getting Started**

This booklet introduces you to the Automatic Resampling process in TNTmips<sup>®</sup>. This process uses georeference control point information to perform simple rectification of distorted images and to transform a raster image into a desired geographic coordinate system. The exercises cover the various options for controlling the size, extents, and orientation of the rectified image, as well as different resampling methods and geometric transformation models. Warping of distorted vector or CAD objects is also briefly introduced.

**Prerequisite Skills** This booklet assumes that you have completed the exercises in the tutorial booklets *Displaying Geospatial Data* and *TNT Product Concepts*. Those exercises introduce essential skills and basic techniques that are not covered again here. You will also find the concepts introduced in the tutorials *Georeferencing* and *Introduction to Map Projections* helpful in understanding image rectification. Please consult those booklets for any review you need.

**Sample Data** The exercises presented in this booklet use sample data that is distributed with the TNT products. If you do not have access to a TNT products DVD, you can download the data from MicroImages' web site. In particular, this booklet uses sample files in the RECTIFY and CB\_DATA data collections.

**More Documentation** This booklet is intended only as an introduction to rectifying and resampling raster images. Details of the process can be found in a variety of tutorial booklets, color plates, and Quick Guides, which are all available from MicroImages' web site.

**TNTmips® Pro and TNTmips Free** TNTmips (the Map and Image Processing System) comes in three versions: the professional version of TNTmips (TNTmips Pro), the low-cost TNTmips Basic version, and the TNTmips Free version. All versions run exactly the same code from the TNT products DVD and have nearly the same features. If you did not purchase the professional version (which requires a software license key) or TNTmips Basic, then TNTmips operates in TNTmips Free mode. The Automatic Resampling process is not available in TNTview or TNTatlas. All the exercises can be completed in TNTlite using the sample geodata provided.

Randall B. Smith, Ph.D., 19 August 2013 © MicroImages, Inc. 1998–2013

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## Welcome to Rectifying Images

In most geographic data sets it is useful to integrate planimetric map data with aerial or satellite imagery. A correctly processed digital map is free of significant geometric distortion and conforms to the projection and coordinate system of the original map. Raw digital images, on the other hand, are not aligned with any conventional geographic coordinate system, and they commonly contain internal geometric distortions that result from the image acquisition process. These distortions can arise from tilt of the sensor plane, variations in sensor altitude, Earth curvature, lens distortion, and terrain relief, among other causes. As a result the raw images do not have a simple "map-like" geometry, and accurate map relationships cannot be derived from them.

The Raster Resampling process (sometimes called warping or "rubber sheeting") changes or rectifies the geometry of a raster image using the locations of ground control points that provide georeference control for the image. Depending on the geometric transformation model you select, the process can remove or reduce internal geometric distortions in the image and reorient and differentially rescale it so that the lines and columns in the output raster are parallel to the axes of a specific geographic coordinate system. Each input raster is processed separately and each must be georeferenced. Control points must be accurately located, sufficient in number for the transformation model selected, and distributed uniformly across the image.

Image rectification / reprojection is not required in all instances. Satellite imagery of low-relief areas may have minimal internal distortions. The Display process in TNTmips can overlay georeferenced layers with different map projections and coordinate systems with reasonable registration. However, if these raster layers will be used together routinely, resampling to a common map projection can significantly speed up display times.



 STEPS
 ☑ start TNTmips
 ☑ choose Image / Resample and Reproject / Automatic from the TNTmips menu

For the sake of brevity, and because multiple input rasters are processed separately, discussions of the resampling process in the remainder of this booklet refer to "the input raster" and "the output raster", regardless of the number of rasters being used.

The exercises on pages 4-9 introduce the Automatic Resampling process, and demonstrate various options for determining the cell size, orientation, and extents of the output raster. Pages 10-11 discuss the three options for interpolating the cell values in the output raster. Geometric transformation models are discussed on pages 12-17. Vector warping is covered on page 18. and a review and references are found on page 19.

To simply rescale, rotate, or flip a raster image without reference to geographic coordinates, use the Raster Extract process (Image / Extract), which allows these operations via the controls on the Zoom/Orient tabbed panel.

## Automatic Raster Resampling Window

#### STEPS

- ☑ click [Select Rasters...] on the Rasters panel of the Raster Resampling window
- use the standard File / Object Selection window to select objects TM7, TM4, and TM2 from the SANBRUNO Project File in the RECTIFY data collection
- on the Settings Panel, select From
   Georeference from the Model menu
- ☑ select Nearest Neighbor from the Method menu
- ☑ select Entire Input from the Extents menu
- ☑ select Manual from the Cell Size menu
- ☑ select Projective North from the Orient menu

Use the Display process (Main / Display from the TNTmips menu) to view the input and output objects for these exercises.

The Model menu provides a choice of different geometric transformation models.

Use the Method menu to choose one of three methods for interpolating cell values for the output raster.

The Extents menu provides <sup>/</sup> several methods for setting the geographic extents of the output raster.

Keep the current settings and continue to the next page.

The Rasters panel on the Raster Resampling window allows you to select the input raster(s) for resampling and lists pertinent spatial and georeference information. Resampling options are set using the menus on the Settings tabbed panel. Choices on these menus set the methods for determining the cell size, orientation, and geographic extents of the output raster, as well as the geometric transformation model and the method for interpolating output cell values. You may have found that the choices specified in the step list on this page were already selected; these are the initial default selections for each menu. However, if you make a different choice from a menu, that choice is saved as the default selection for the next session. Always check each of the parameter menus to confirm that your desired menu choice is selected.

The Orient menu offers options for orienting the output raster relative to the output projection. Choices on the Cell Size menu determine the method used to set the cell size for the output raster.

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- Kaster	. Kesampling using be	oreterence (;			
Rasters	Settings	< /			
Model	Fron Georeference	Cell Siz	e Manual 💌		
, Hethod	Nearest Neighbor 💌	Orient	Projective North 💌		
Extents	Entire Input 💌	Pyramid	Automatic 💌		
Referen	ce Raster				
Referen	ce System Same as	input			
Cell 9	Size (meters)	Ina	ge Size		
Line	2	8.49 Lines	592		
Column	2	28.53 Colum	ins 510		
Extent	ts				
Coordin	nates NAD27 / UTM	zone 10N (CM	123H)		
Easting	y E	642982.96 to	557533.26		
Northin	ng 41	.57346.27 to	4174212.35		
Geoid Height					
Compres	sion Uncompressed	•			
Queue	Job Save Job	. Run	. Exit		

# **Rectifying to the Input Map Projection**

You will probably use the Automatic Resampling process most often to reproject a georeferenced raster into the coordinate reference system specified in its georeference subobject. To do so, use the default option on the Orient menu (Projective North) and the default Reference System option (Same as input). Horizontal lines of cells in the output raster are then parallel to the x axis of the input geographic coordinate system, and vertical columns are parallel to the y coordinate axis. The input rasters used in this exercise are extracts of a Landsat Thematic Mapper scene georeferenced to the Universal Transverse Mercator coordinate system (Zone 10N), so the output raster set is aligned to the UTM system.

When you choose Manual as the Cell Size menu option, the Cell Size fields are automatically set from the input object's georeference information; you can edit these values if desired to change the cell size for the output product. The cell size, geographic extents, and output projection then determine the number of lines and columns in the output raster. STEPS

- Ø press [Run...]
- use the standard File / Object selection procedures to name a new Project File and the output raster objects

	-	 _	
Reference	Raster		

Use the default Reference System option to warp the input raster into the coordinate reference system specified in its georeference subobject.

-Cell S	Gize (meters) —	
Line		28,49
Column		28,53

In this exercise, we preserve the spatial resolution of the original imagery when creating the resampled output set.



Output raster set (warped and reoriented to the UTM coordinate system), displayed with UTM grid tick marks along the border for emphasis.

RGB display of input raster set with R = TM7, G = TM4, and B = TM2.



# Warping to a New Map Projection

Clicking the Reference System button opens the Coordinate Reference System window, which allows you to choose a different output coordinate reference system.

Reference Raster	
Reference System	• Same as input
-Cell Size (meters	s)
Line	28,49
Column	28,53

STEPS

- ☑ click [Reference System...]
- ☑ in the Coordinate Reference System window. on the Predefined panel navigate to the National and Local / United States / California arouping

You can also warp the input raster to a coordinate reference system other than the one in which it is georeferenced. Use the Coordinate Reference System window to choose from among many predefined coordinate reference systems, coordinate systems, and datums. In this exercise the input raster set is reoriented to the predefined NAD27 / SPCS27 California Zone 3 (ftUS) coordinate reference system.

Warping a raster to a different coordinate reference system commonly results in a significant rotation of the image, as well as other internal changes in its geometry. If you warp the entire image (as in this exercise), the edges of the resampled image are not parallel to lines and columns in the output raster. The warped and rotated image is embedded in a raster that is somewhat larger than the original, with triangular "blank" (nonimage) areas at the corners. (The blank areas are flagged in the null mask so they can be rendered transparent when the

Coordinate Reference System (50007		
Predefined Coordinate System   Datum   Projection   Details		
🗄 Arizona		
🗄 Arkansas		
🗆 California		
NAD27 / SPCS27 California zone 1 (m)		
NAD27 / SPCS27 California zone 2 (m)		
NAD27 / SPCS27 California zone 3 (m)		
NAD27 / SPCS27 California zone 4 (m)		
NAD27 / SPCS27 California zone 5 (m)		
NAD27 / SPCS27 California zone 6 (m)		
NAD27 / SPCS27 California zone 7 (m)		
NAD27 / SPCS27 California zone 1 (ftUS)		
NAD27 / SPCS27 California zone 2 (ftUS)		
NAD27 / SPCS27 California zone 3 (ftUS)		
NAD27 / SPCS27 California zone 4 (ftUS)		
NAD27 / SPCS27 California zone 5 (ftUS)		
FI		
Current: NAD27 / SPCS27 California zone 3 (ftUS)		
Save As		
•		

- ☑ choose NAD27 / SPCS27 California zone 3 (ftUS), then click [OK]
- ☑ choose Run in the Raster Resampling window and name the output raster objects

Use of the Coordinate Reference System window is introduced in the Coordinate Reference Systems tutorial.

raster is displayed.)



Output raster set in the NAD27 / SPCS27 California Zone 3 (ftUS) coordinate reference system.

### Warping to a Reference Raster

A raster that is already aligned to a geographic coordinate system can be selected as a Reference Raster to control the cell size, orientation, and/or extents of the output raster created by the resampling process. Cell size and orientation are linked in this instance; choosing Match Reference from the Cell Size menu automatically selects Match Reference on the Orient menu (and *vice versa*). With these

options selected, the output raster assumes the cell size and orientation of the reference raster.

You can use the Match Reference

option on the Extents menu to trim the output image to the exact extents of the reference raster. This is an appropriate choice if the reference raster is wholly contained within the area of the input raster image (as in this exercise). If the reference and input rasters only partially overlap, you may want to select the Overlap Reference option to output only the area common to both.

Reference raster MAP, aligned to the UTM coordinate

system, with a cell size of 20 meters.

choose Match
 Reference from the Cell
 Size menu

STEPS

- When prompted, select the MAP object from the SANBRUNO Project File
- ☑ choose Match Reference from the Extents menu

lodel	From Georeference 💌	Cell Size	Match Reference 💌		
lethod	Nearest Neighbor 💌	Orient	Match Reference 💌		
xtents	Match Reference 💌	Pyramid	Autonatic 💌		
Reference Raster sanbruno.rvc / MAP					
Referen	ce System From refere	nce			

✓ run the resampling process

 Cell Size (neters)

 Line
 19,966339502486232

 Column
 19,961271116394521

The output cell size is set automatically when you use a reference raster to control the cell size and orientation of the output. The reference projection overrides any previously selected coordinate reference system.



Raster set resampled using the reference raster to specify cell size, orientation, and output extents.



# **Setting Output Extents and Raster Size**

#### STEPS

- ☑ choose Projective North from the Orient menu
- ☑ choose By Image Size from the Cell Size menu
- ☑ enter 600 in the Lines field and 409 in the Columns field in the Raster Size pane
- ☑ choose User Defined from the Extents menu
- ☑ the previously-selected NAD27 / SPCS27 California zone 3 (ftUS) coordinate reference system is once again active in the Reference System field
- enter the following extents ranges: Easting: 1425825 to 1455515; Northing: 398700 to 442400
- ☑ run the resampling process



Output rasters in State Plane 1927 coordinate system, with extents specified in the Extents panel. Compare with image on page 6.

We have covered several options for specifying the extents of the output raster, including Entire Input, Match Reference, and Overlap Reference. The final option is User Defined. When you select this option from the Extents menu, the Extents controls become active, allowing you to enter exact geographic extents for the output raster using any available coordinate reference system. Click the Coordinates button to open the Coordinate Reference System window to make your selection.

In some instances you may want the output raster to have a specific size in lines and columns. The By Image Size option on the Cell Size menu provides this capability. The line and column cell sizes are then determined by the raster size and output extents.

The reference raster used in the last exercise is still selected and available for use. However, the Reference Raster button is dimmed, showing that the raster is not in use with the current settings. The previously-selected State Plane coordinate reference system is once again active.

1	\				
Model From Geo	reference 💌	Cell Size	By Image Size 💌		
Method Nearest	Neighbor 💌	Orient	Projective North 💌		
Extents User Def	ined 🔽	Pyramid	Automatic 💌		
Reference Raster	•••• sanbr ino • r	vc / MAP			
Reference System	•••• NAD27 7 SP	CS27 Califo	ornia zone 3 (ftUS)		
-Cell Size (fee	t (US survey))	Inag	e Size		
Line		Lines	600		
Column		Colum	ns 409		
Extents					
Coordinates	NAD27 / UTH zor	ne 10N (CM	123H)		
Easting	14258	325.00 to	1455515.00		
Northing	3987	700.00 to	442400.00		
Geoid Height					
Compression Uncompressed					
Queue Job	Save Job	Run	Exit		
	\				

You can use the Queue Job and Save Job buttons to run resampling operations under the TNT job processing system. See the Technical Guide entitled *System: TNTmips Job Processing System* for details.

### **Orienting to a Direction**

The vertical axis of an input raster's map coordinate system (such as State Plane or UTM) may not be parallel to the local direction of true north. The Orient menu allows you to use the georeference information to align the output raster with any of the four cardinal compass directions at the top. These options are most useful when the input raster is already aligned with a map coordinate system, and you want to reorient it with north at the top.

In this example, the edges of the input raster set coincide with lines of equal latitude (horizontal) and longitude (vertical), so it is already oriented with north at top. Reorienting it to the State Plane projection would cause a clockwise rotation of a few degrees. Reorienting it with South at Top exactly inverts the image.

📼 Raster	Resampling	using Geore	Ference (30	00)	_ 🗆 ×
Rasters S	Settings				
Model F	ron Georefe	rence 💌	Cell Size	Manual	-
Hethod N	learest Neig	hbor 💌	Orient	Geographic	South 💌
Extents E	intire Input	. ▼	Pyranid	Projective Geographie	North
Reference	e Raster			Geographic	South
Reference	e System	Same as inp	out	Geographic Geographic	East /
-Cell Si	ze (meters)		Inage	Match Refe	ence
Line	24,400	43633145969	1 Lines		572
Column	27,612	12678292460	5 Colum	IS	374
					/



You can orient the output raster with any of the four cardinal directions at the top. STEPS

☑ click [Select Rasters...] on the Rasters panel and select objects PHOTO\_IR, RED, and GREEN from the CB\_TM Project File in the CB\_DATA data collection

Raster Resampling using		
Rasters Settings		
Select Raster(s)		
cb_tm.rvc / PHOTO_IR		
cb_tm.rvc / RED cb_tm.rvc / GREEN		

- ☑ on the Settings panel, choose Manual from the Cell Size menu
- ☑ choose Geographic South from the Orient menu
- ☑ run the resampling process

RGB display of input raster set ( $R = PHOTO_IR$ , G = RED, and B = GREEN) with a 10,000 foot State Plane Coordinate map grid in yellow.



Output raster set reoriented with south at top.

# **Cell Value Interpolation in Resampling**

#### STEPS

- click [Select Rasters...] on the Rasters panel and select object PAN from the SANBRUNO Project File
- ☑ in the Cell Size pane on the Settings panel, enter 2.00 in both Line and Column text fields
- ☑ select Projective North from the Orient menu
- make sure that Nearest Neighbor is still selected in the Method menu
- ☑ run the resampling process

Method	Nearest Neighbor 💌
Extents	Nearest Neighbor 🛛
	Bilinear
Referen	Bicubic
D-C	Bicubic Sharper -
Ket eren	Bicubic Smoother
-Cell S	Lanczos 4x4 –

- select Bilinear from the Method menu and run the process again
- ☑ repeat with Bicubic as the resampling method

Superimposed portion of rectified \_\_\_\_\_ output raster. Bold outline indicates current target cell for which a value is being interpolated.





The Automatic Resampling process uses several steps to create the transformed output raster. First, the geometric transformation procedure (described subsequently) creates a "blank" rectified raster with the proper extents and scale (cell size). Then a cell value is determined for each cell in the rectified raster. To do so, the geometric transformation is reversed for each output cell in order to determine its position in terms of the original raster line and column coordinates. The target output cell may be larger or smaller than an input cell, and it may overlap several input cells. The output cell value must therefore be calculated (interpolated) from some combination of the surrounding input cells.

The Method menu offers several options for interpolating output cell values. The Nearest Neighbor, Bilinear, and Bicubic methods are illustrated in the diagram below and are discussed on the next page.



# **Resampling Methods**

**Nearest Neighbor** Each output cell value in the nearest neighbor method is the unmodified value from the closest input cell. Less computation is involved than in the other methods, leading to a speed advantage for large input rasters. Preservation of the original cell values can also be an advantage if the resampled raster will be used in later quantitative analysis, such as automatic classification. However, nearest neighbor resampling can cause feature edges to be offset by distances up to half of the input cell size. If the raster is resampled to a different cell size, a blocky appearance can result from the duplication (smaller output cell size) or dropping (larger cell size) of input cell values.

**Bilinear** An output cell value in the bilinear interpolation method is the weighted average of the four closest input cell values, with weighting factors determined by the linear distance between output and input cells. This method produces a smoother appearance than the nearest neighbor approach, but it can diminish the contrast and sharpness of feature edges. It works best when you are resampling to a smaller output cell size

**Bicubic** The bicubic method calculates an output cell value from a  $4 \ge 4$  block of surrounding input cells. The output value is a distance-weighted average, but the weight values vary as a nonlinear function of distance. This method produces sharper, less blurry images than bilinear interpolation, but it is the most computationally intensive resampling method. It is the preferred method when resampling to a larger output cell size. Two variants are also provided to produce sharper and smoother results.

Nearest neighbor resampling is the only method that is appropriate for categorical rasters, such as class rasters produced by the Automatic Classification process. Cell values in these rasters are merely arbitrary labels without numerical significance, so mathematical combinations of adjacent cell values have no meaning. Raster PAN resampled from a cell size of 10 meters to 2 meters using three resampling methods.



**Nearest Neighbor** 



Bilinear



Bicubic

# **Rectifying a Color Infrared Airslide**

#### STEPS:

Use the Display process to examine the following:

- RGB display of objects NIR, RED, and GREEN from the SECT32 Project File in the RECTIFY data collection
- ☑ single-raster display of object SECTMAP in the SECT32 Project File

Color infrared photo of Section 32 with locations of ground control points used for georeferencing. The image was georeferenced to the UTM coordinate system using a UGSG Digital Orthophoto Quad image with 1-meter cell size.

The northern and southern section/ lines are not parallel in the photo, and appear to converge toward the west (compare with the map below). This indicates that the camera was not pointed straight down, but was tilted slightly toward the west when the photo was taken.

The remaining exercises use a color-infrared airslide of a mile-square section of agricultural and residential land in eastern Nebraska. The airslide exhibits several types of distortion, and the exercises examine the effects of different geometric transformation models in attempting to rectify this image.





Several of the section lines also are curved outward slightly. Some of the areas of curvature coincide with topographic ridges, suggesting that this is an effect of relief displacement. Some of the outward curvature may also be a radial distortion resulting from imperfections in the camera lens.

Topographic map (object SECTMAP) covering Section 32, resampled to conform to the UTM coordinate system. Note the nearly square shape defined by the roads bounding the section. The residential development in the southeastern quarter of the section was not present when this map was compiled.

### **Geometric Transformation Models**

To alter the geometry of the input raster, the Automatic Resampling process analyzes the locations of the ground control points that were assigned in the georeference process. These are points in the image with known coordinates in a standard coordinate reference system. The process compares the geographic coordinates of the control points to the locations predicted by the geometric transformation model you have selected. The results are used to determine numerical coefficients for coordinate transformation equations that convert the original image to the desired coordinate reference system.

The Automatic Resampling process incorporates all of the geometric transformation models that are available in the Georeference process for assessing the quality of control point locations. Each transformation model requires a minimum number of control points for solution. The minimum number of control points provides a single, unique solution, but any errors in control point locations directly impact the transformation. If additional control points are available, the process computes a best-fit transformation using least squares adjustment. This procedure chooses the set of coefficients for which the sum of the squared residual errors (deviations between predicted and actual locations in the final coordinate system) is a minimum.

The quality of the rectification result depends on the number, accuracy, and distribution of the control points and the choice of transformation model. Care in the georeference process is the best guarantee of success in rectification. Position control points so that they cover most of the image. Adjust control point positions to minimize the residual values (error estimates resulting from the least squares adjustment) for each control point. Appropriate uses for some of the transformation models are discussed on the following pages.

### STEPS

- ☑ click [Select Rasters...] on the Rasters panel and select objects NIR, RED, and GREEN from the SECT32 Project File
- ☑ choose Bicubic from the Method menu
- ☑ select Match Reference from the Cell Size menu
- ☑ when prompted, select object SECTMAP from the SECT32 Project File

The From Georeference option selects the transformation model that was saved with the control point locations in each object's georeference subobject. This choice potentially allows different transformation models to be applied to different raster objects in the input list.



Each of the other model choices is applied globally to all input raster objects, regardless of the model used in the georeference process. The Rational Polynomial method can be used to orthorectify certain satellite images. See the tutorial entitled *Orthorectification using Rational Polynomials.* 

Keep the current settings and proceed to the next page.

# Affine Model

#### STEPS

- ☑ choose Affine from the Model menu
- ☑ run the resampling process

In this and the following exercises we process the entire input image, but use the SECTMAP raster to control the cell size and orientation of the output image. The image is resampled from a cell size of about 3.37 m to an output cell size of 4.0 m.

### Affine Transformations



The affine transformation model projects coordinates from one plane (defined by the original coordinate system) to another *parallel* plane (defined by the output coordinate system). An affine model can incorporate any or all of the transformations illustrated: translation, rescaling, rotation, and skew (or shear) of the image. Rescaling can accomodate a separate scale factor for each of the two coordinate axis directions. Any set of parallel lines in the source image remain parallel in the output image. The affine model requires a minimum of three control points that do not fall on a single straight line.

The affine model is appropriate when you need to convert a planimetric map raster (or an already-rectified image) from its original coordinate system and map projection to a new planar coordinate system (for example, UTM to State Plane coordinates). It may also give satisfactory results if you are rectifying a vertical aerial or satellite image of a small area with little topographic relief (so that the surface approximates a plane, and there is little or no tilt displacement or relief displacement).



The affine transformation rotated and rescaled the CIR image, but did not correct the curvature and convergence of the section lines (the effects of more complex tilt distortion and relief displacement).

# **Plane Projective Model**

The plane projective model transforms coordinates between any pair of source and target planes, including *nonparallel* planes. It employs a perspective projection: projection lines linking input and output coordinate locations emanate from a single central view point, analogous to the imaging geometry of an aerial camera. For this reason, the plane projective model is commonly used to rectify nonvertical aerial images of relatively flat terrain.

The plane projective model incorporates all of the transformations found in the affine model. However, the only lines that remain parallel in both the distorted and rectified images are those that are parallel to the line of intersection between the two planes. The plane projective model requires a minimum of four noncolinear control points.



The plane projective transformation corrected the tilt distortion found in the original image. The north and south section lines are now nearly parallel. However, the subtle curvature of these lines shows that some distortion arising from relief displacement and/or lens effects still remains. Distortion due to relief displacement is relatively minor for this image because vertical relief is small (about 110 feet) compared to the image's horizontal dimensions.

### STEPS

- ☑ choose Plane Projective from the Model menu
- ☑ run the resampling process



The plane projective model transforms coordinates in one plane to another nonparallel plane using a perspective projection.

Oblique perspective view of a square results in a trapezoidal shape. The plane projective model can rectify this simple tilt distortion.



## **Polynomial Models**

STEPS

- choose Order 3
   Polynomial from the Model menu
- ☑ run the resampling process

The minimum number of required control points increases with the polynomial order:

Order 2: 6 control points Order 3: 10 control points Order 4: 15 control points

Hypothetical plot of input versus output control point position in one direction, illustrating fit with polynomials of different order.



Input X coordinate

Polynomial transformations of the test image produce very similar results for all three orders, probably because of the small image area, dense network of control points, and small amount of terrain distortion. The Order 3 polynomial appears to produce the best result (shown here), comparable to the result from the plane projective transformation. Several of the section lines are still bowed outward, an indication of uncorrected terrain distortion.

The Polynomial transformations can correct *nonlinear* distortions in a raster image, as well as the linear distortions handled by the models discussed previously. Polynomial equations are used to relate control point positions in the distorted image coordinates to corresponding positions in the output geographic coordinate system. The control point information is used to calculate a best-fit set of coefficients for the terms in the equations. The *order* of the polynomial model is the highest exponent used in the equations, and specifies the allowed complexity of the fit, as shown for one direction in the illustration below left.

An Order 2 polynomial describes a fit with one sense of curvature (concave or convex) in any direction. This model can correct for radial lens distortion or distortion arising from curvature of the Earth in highaltitude or satellite scenes of large areas. An Order 3 polynomial allows one change in sense of curvature in any direction, and an Order 4 polynomial allows for an even more complex fit. These models can correct more complex image distortions, but may introduce distortion in areas between control points, especially around the edges of the image.



### **Piecewise Affine Model**

The transformation models discussed previously all compute a global best-fit solution for the entire image. They are best tailored to remove smoothly varying distortions. Distortions that change significantly over small areas are not corrected. In fact, a local distortion that affects the positions of one or two control points will influence the overall fit as much as other correctly modeled points. As a result, the local distortion introduces a smaller component of distortion throughout the entire rectified image.

The Piecewise Affine model offers an alternative approach. Each control point is assumed to be in the correct position, and the points are used to segment the image into a network of triangles. An affine transformation is then computed separately for each triangle. A single distorted control point location only affects the immediately surrounding triangles. At least six control points are required, but larger numbers produce better results.



#### STEPS

- ☑ choose Piecewise Affine from the Model menu
- ☑ run the resampling process

Example image partitions using the control points for the test image.



The Delauney triangulation procedure is used to compute the optimum triangular network, with some extrapolated boundary points added for completeness.

The Piecewise Affine transformation of the test image produces a slight improvement over all of the previous methods. Because of the large number of control points and the gentle relief, the method is able to correct some of the terrain distortions, producing straighter section boundaries. This method is also useful for rectifying scanned map mosaics that were assembled from pieces with various sources and scales (such as some property maps).

The highly localized and variable relief displacement distortion found in aerial photographs of high-relief areas cannot be corrected using the Automatic Resampling process. Rectification of these images to a map geometry (orthorectification) requires the use of stereo images or an accurate digital elevation model (DEM). See the tutorial entitled *Making DEMs and Orthophotos* for more information.

# **Reprojecting Vector or CAD Objects**

#### STEPS

- choose Geometric / Reproject from the TNTmips menu
- ☑ in the Geometric Warping window, click Select...
- Select vector object ROADS from the SECT32 Project File
- choose Plane Projective from the Model option button
- ☑ click [Run] and name the output object

The Geometric Warping process provides a subset of the transformation models that are available in the Automatic Resampling process for rasters.



The ROADS object was created in the Spatial Data Editor by tracing the roads and fence lines from an ungeoreferenced version of the raw SECT32 image. It was then georeferenced to UTM using a USGS Digital Orthophoto Quad image.

Vector object ROADS after warping to UTM using the Plane Projective model, ~ displayed with green line color over the SECT32 map object.

The Geometric Warping process permanently reprojects element locations in a vector or CAD object to the selected coordinate reference system. You can use this process with the From Georeference model option to reproject geometric objects from one coordinate reference system to another, typically to match that of other data you are using frequently in a project. Although the TNTmips Display process can reproject a vector object on the fly to overlay other objects with a different reference system, the redisplay time for a large vector object may be significantly longer when reprojection is required.

If a vector (or CAD) object is created from a distorted, nongeoreferenced raster image, the resulting object incorporates the spatial distortions of the parent object. These distortions remain even after

> georeference control points are assigned to the vector object. For objects with control point georeference, the Geometric Warping process provides a subset of the geometric transformation models discussed previously that can be used to rectify the object.



Obviously, a better strategy is to georeference and rectify source imagery *before* creating a vector overlay. The vector object is then automatically georeferenced and aligned to the desired coordinate reference system.

### **Review and References**

There are several common situations in which you should use the Automatic Resampling process:

- to reproject a set of georeferenced raster images to a common coordinate reference system and cell size to facilitate spatial analysis, classification, change detection in multidate imagery, or other scene-to-scene comparisons of individual cell values. This includes scanned topographic and planimetric maps that have been georeferenced but not yet aligned to the desired coordinate system.
- to remove or reduce certain types of simple geometric distortions from aerial or satellite imagery, producing a more map-like image geometry.

You do *not* need to resample component images before making a mosaic unless different images exhibit different types of distortion. The Mosaic process applies a single selected geometric transformation model to rectify all georeferenced images to a common coordinate reference system.

Successful rectification begins with careful georeferencing of the images. You need to determine the types of distortion present in the image and choose the appropriate geometric transformation model. Use this model in the georeference process to evaluate residual errors in control point locations, and again in the Automatic Resampling process for the actual rectification.

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### Index

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2 Des

affine transformation	14
bilinear interpolation	10,11
control points	3,13,16
cubic convolution interpolation	10,11
extents, geographic	4,7-9
geometric transformation models.	13-17,19
georeference	.3,5,9,13,19
interpolation	4,10,11
bilinear	
cubic convolution	10,11
models, geometric transformation	13-17
map projection, orienting to	5,6
orientation	4
to a direction	9
to a map projection	5,6
to a reference raster	7

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nearest neighbor resampling	
piecewise affine transformation	17
perspective projection	15
plane projective transformation.	15
polynomial transformation	16
reference raster	7
relief displacement	12,14,15,17
resampling	
rubber sheeting	3
terrain distortion	16,17
See relief displacement	
tilt distortion	14,15
vector object, warping	
scale	4,7
warping	3,6,7,18

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